

Optimization of the Separation of Sulfur Hexafluoride and Nitrogen by Selective Adsorption Using Monte Carlo Simulations

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We present molecular simulations to find the optimal conditions for the separation by adsorption of SF_6 from a gaseous mixture with N_2 , a mixture of key interest in electrical applications. The effect of pore size, pressure, and mixture compositions on the selective adsorption of SF_6 was investigated by using Grand Canonical Monte Carlo simulations with simple fluid models and a simplified model of MCM-41. Simulations performed with multisite fluid models confirm that general trends are predicted using simple models, including a maximum in SF_6 selectivity for pore diameters around 1.1 nm. Simulations were also performed using two atomistic models of zeolite-templated carbon (ZTC), FAU-ZTC, and EMT-ZTC, materials with average pore sizes close to 1.1 nm, obtaining high selectivities for both materials. Selectivities for FAU-ZTC are approximately four times higher than the best materials published for this mixture separation, opening excellent opportunities to use it for recovering SF_6 from SF_6/N_2 mixtures. © 2010 American Institute of Chemical Engineers *AIChE J.*, 57: 962–974, 2011

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Introduction

Sulfur hexafluoride (SF_6) is a colorless, odorless, nontoxic, and nonflammable gas. It is mainly used in gas insulated substations and related equipment in electrical transmission

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and distribution systems because its arc quenching properties and high dielectric strength. Despite these unique properties, SF₆ is a very potent greenhouse gas (GHG); its global warming potential is 22,000 larger than carbon dioxide's and its atmospheric lifetime is estimated to be 3200 years.^{1,2} Therefore, almost all SF₆ emissions need to be avoided because of its long-term effects in the environment. Hence, there have been numerous efforts to reduce emissions from facilities using SF₆.^{3,4} Besides, there are numerous research studies aimed at finding an alternative gas for insulation of electrical equipment, but a suitable substitute for SF₆ for some key applications is yet to be found.⁵⁻⁷

One of the main options to diminish SF₆ emissions is mixing it with other gases to reduce the overall amount of SF₆ used, while keeping the desired properties of the pure fluid. Nitrogen is the preferred gas for these mixtures, for two main reasons: mixtures of SF₆ and N₂ with a low concentration of SF₆ still maintain the high dielectric strength of pure SF₆; and nitrogen is a cheap gas, making the overall process cheaper and environmentally friendlier.^{8,9} However, a mixture of sulfur hexafluoride and nitrogen increases the difficulty of recovering and recycling the SF₆, as in this case a process able to effectively separate SF₆ and N₂ is required. The process becomes more complex as the amount of SF₆ in the mixture becomes very small.⁸ Besides, the high concentration of N₂ in the gas mixtures used for insulation of electrical equipment makes the separation by liquefaction an impractical process, since it requires an excessive amount of energy to cool down and pressurize the mixture; hence, alternative processes are required.

There are some works available in the literature dealing with the separation of the SF₆/N₂ mixtures, being most of them experimental studies using adsorbents. The separation of SF₆ from N₂ by adsorption is achieved either by molecularly sieving the N₂ or by preferentially adsorbing the SF₆ at low pressures. Toyoda et al. used the molecular sieving effect of a Ca-A type zeolite with an effective diameter of 0.5 nm to adsorb N₂ but not SF₆.¹⁰ Yamamoto and coworkers proposed a system of polyimide membranes.⁹ They analyzed the influence of different operating variables, such as the gas feeding pressure and the membrane temperature, on the gaseous mixture separation. Murase and coworkers selectively adsorbed SF₆ from a mixture with nitrogen by using a Na-X type zeolite with a nominal pore diameter of 1.0 nm.¹¹ They proposed that the filter, besides separating, could also be used as a temporary storage medium. Shiojiri et al. separated F-gases from gaseous mixtures containing N₂ by making use of the differences in surface diffusion, using a porous Vycor glass membrane.¹² Inami et al. studied the theoretical limit for SF₆/N₂ separation by liquefaction and found that the liquid SF₆ recovery efficiency decreases greatly at higher N₂ content.⁸ They discussed that for SF₆ contents below 10%, even at a temperature below -50°C, the SF₆ recovery was almost zero.

Although available data on adsorption of pure components is widely accessible, the number of experimental studies on adsorption of mixtures is very scarce. This is mainly due to the difficulty of performing adsorption experiments with mixtures. The adsorption can be accurately determined for pure compounds by measuring the weight change of the adsorbent, whereas for mixtures additional experiments are

needed to determine the composition of the adsorbate.¹³ However, the development, design, and operation of separation processes by adsorption require knowledge of the physical properties of the mixture to be separated, such as the equilibrium data. A way to overcome this difficulty is by using molecular simulations in a synergetic manner with experiments: once an accurate model for the fluid and the material is found, and experimental data for the pure fluid are appropriately described, simulations of the mixture can then be used to find the optimal conditions for the separation.

The objective of this work is twofold: (1) to use molecular simulations, with simple models for the fluid and the adsorbent, as a fast way to find the optimal conditions for the separation of SF₆ from N₂, and (2) to check the validity of the results obtained with simple models with more realistic materials, searching for the best material to separate this mixture. In this work, a complementary view to the usual optimization process is given: we use molecular simulations to illustrate an optimization procedure for the separation of SF₆ and N₂ by modifying operating variables, mainly the bulk pressure and mixture composition, and atomistic level parameters, essentially the pore diameter, with the same adsorbent material. The final objective is to find the optimal pore diameter to achieve the separation by adsorption of SF₆ from a SF₆/N₂ stream. It is shown how molecular simulations can be used as a tool to optimize and design separation processes by using its predictive capabilities in a fast and reliable manner. The material used in the first stage is a cylindrical porous adsorbent, namely MCM-41. It consists of a hexagonal array of monodisperse pores formed by amorphous silica (SiO₂). This material was chosen for two main reasons: because of its simple geometry, with cylindrical pores (straightforward to be modeled with simple simulation force fields) and because of its potential as an adsorbent material for several industrial processes. MCM-41 may reach an exceptional porosity, up to 80%, making it an excellent potential adsorbent material to be used in gas storage systems, separation processes, and catalysis.¹⁴⁻¹⁶ MCM-41 belongs to a family of uniform mesoporous silica materials discovered by Mobil Corporation^{17,18} and it can be synthesized with narrow tunable pore size distributions, from the microporous to the mesoporous range.^{19,20} Pore size tunability makes this kind of materials a good model for investigating fundamental features of adsorption such as the effects of pore size for a given geometry, and a starting point to achieve a methodical optimization.

Furthermore, the ideal smooth cylindrical pore is chosen in this work for its instructive value. Although a cylindrical pore is an overly simplistic model of real pores, it provides a useful estimate in studying the effects of confinement on selectivity. This sort of fundamental study may provide guidelines in choosing materials with the appropriate pore size for gas separation applications.²¹ Throughout the first part of this article, we have chosen a simplified model of MCM-41. We have used this model to find the optimal diameter to achieve the maximum selectivity of SF₆. Simulations were later performed with more realistic materials, using atomistic models of zeolite-templated carbon materials (ZTC), chosen to assess the predictability of the results obtained with the cylindrical pore model for the optimal diameter.

ZTCs are porous carbons with a well-tailored microporous structure obtained by using the template carbonization method employing a zeolite as the template.^{22,23} The pores and walls of the zeolite become the walls and pores of the carbon replica, respectively, therefore the carbon structures obtained by this method have very high-surface areas and periodic ordered structures.²⁴ We have chosen these templated materials in the second part of this work as a possible material for the separation of SF₆ and N₂ because, in addition to having the appropriate pore diameter, these carbon materials have good stability at high temperatures and they have a low affinity for water.²⁵ Besides the high mechanical properties of ZTCs make them suitable to work at high pressures.²⁶ These characteristics offer unique advantages over inorganic molecular sieves and make the applications of such materials very attractive. In this article, we simulated the adsorption on the pores of hexagonal (EMT) and cubic (FAU-Y) zeolite-templated carbons, which have an average pore size close to 1.1 nm.²⁷

The rest of the article is organized as follows: the fluid and pore models used in the simulations are described in the following section. Next, we give the essential information on the simulation method used for computing the adsorption behavior. Then, we show the influence of the diameter on the separation process of sulfur hexafluoride, and find the optimal diameter for selecting SF₆ over N₂. Besides, we discuss the effect of using two different kinds of models for the fluid molecules on the simulation results. Then the results for the optimal diameter for the separation are contrasted with a more realistic material by using two model Zeolite-Templated Carbons.

Models

Fluid models

We have considered two sets of models for each fluid molecule. The first one consisted of simple 1-site Lennard-Jones (LJ) model, which means representing the fluid molecules by spheres with van der Waals type attractive and repulsive interactions; this set of models was used for the initial stage of the optimization procedure. Although predictions from these models are usually less accurate than those obtained with more refined force fields, the 1-site model requires less computational resources while providing a first good approximation for the appropriate separation conditions. This set of models was used to run a series of adsorption isotherms with a broad range of pore diameters and a smaller separation step between each diameter. The results obtained from the 1-site model were further refined by using a second set of models, in which we introduced more degrees of freedom to the molecular structure to get more realistic predictions. For this second set, we have used a flexible 6-site model for sulfur hexafluoride developed by Olivet and Vega,²⁸ and a 2-site model for nitrogen developed by Galassi and Tildesley.²⁹ The values of the LJ parameters for each model are provided in Table 1.

Several LJ parameters for 1-site SF₆ and N₂ models are available in the literature.^{30,31} Some of them have been adjusted to predict the vapor–liquid coexistence region, while others are more accurate for the estimation of transport

Table 1. Lennard-Jones Parameters for the Simulated Force Fields for N₂ and SF₆ Used in This Work

Force Field	σ (Å)	ϵ/k_b (K)
1-site SF ₆	4.650	251.1
Multisite flexible SF ₆ (six F)	2.769	73.13
1-site N ₂	3.582	98.83
Multisite N ₂ (2 N)	3.310	93.98

Note that in addition to these values, additional parameters are used for the bonds and angles for the multisite models. See text for details.

properties. In this work, the parameters for the LJ potential for both molecules were obtained by adjusting the experimental vapor–liquid equilibrium densities using the soft-SAFT equation of state, using just the reference term of this equation, which is a LJ spherical fluid.^{32,33} The advantage of using this procedure is that the equation is very accurate for these fluids, and in addition, it provides a straightforward relationship between the pressure and the chemical potential, needed for the adsorption isotherms.

In the 1-site model, the interaction energy, U_{inter} , between two molecules i and j , is accounted for by the Lennard-Jones potential.

For multisite models, the SF₆ molecule is represented by different interacting sites. The total intermolecular interaction between two molecules is calculated as the sum of the energies of point-site interactions in each molecule. The model used for SF₆ explicitly includes the flexibility of the molecule; thus, the intramolecular energy for one molecule, U_{intra} , is calculated as a sum of the equilibrium bond and equilibrium angle energies.

$$U_{\text{intra}} = \sum_{\text{bonds}} K_r (r_{ab} - r_0)^2 + \sum_{\text{angles}} K_\theta (\theta_{ABC} - \theta_0)^2 \quad (1)$$

K_r and K_θ are the force constants for the bonds and angles, respectively. r_{ab} is the distance between atoms a and b, and r_0 is the equilibrium distance for that pair of atoms. θ_{ABC} is the angle formed by the atoms A, B, and C, whereas θ_0 is their equilibrium angle.

The multisite model used in this work for SF₆ was the flexible force field proposed by Olivet and Vega.²⁸ In this model, explicit interactions are only considered to occur among fluorine atoms. All interactions involving sulfur atoms are neglected on the assumption that a modified fluorine–fluorine LJ potential could incorporate any sulfur–sulfur or sulfur–fluorine interactions. To account for the flexibility of the molecule, this model uses six harmonic stretching terms for modeling the S–F bonds and twelve harmonic bending terms for modeling the F–S–F angular deformations. This force field was obtained by simultaneously fitting selected vapor–liquid equilibrium (VLE) and transport properties to available experimental data and it has proven to give excellent results for transport properties of SF₆/N₂ mixtures.³⁴ The values of the parameters for the flexible part of this potential are $\theta_0 = 90^\circ$, $K_\theta = 307.36$ kJ/mol rad², $r_0 = 0.1565$ nm and $K_r = 69348.0$ kJ/mol nm².

To represent the diatomic N₂ molecule, we used the model proposed by Galassi and Tildesley.²⁹ This force field uses a

rigid dumbbell representation for N₂ molecules, with a distance between the nitrogen atoms of 0.1089 nm, and the intermolecular interactions are quantified by a LJ potential. The parameters of this potential were fitted to reproduce experimental VLE data.

Solid adsorbents

As mentioned in the introduction, the adsorbent material used in the simulations for finding the optimal diameter was first a porous silica material, MCM-41, and later two Zeolite-Templated Carbons (ZTC).

MCM-41 was represented by a simple cylindrical model, taking the potential form given by Tjatjopoulos.³⁵ This model assumes that the regular hexagonal surface of MCM-41 can be represented by a cylindrical homogeneous surface, in which the interaction sites are continuously distributed on a sequence of concentric surfaces that compose the pore wall.

$$U_{\text{wall}}(r, R) = \pi^2 \rho_s \epsilon_{\text{sf}} \left[\frac{63}{32} \left[\frac{r}{\sigma_{\text{sf}}} \left(2 - \frac{r}{R} \right) \right]^{-10} F \left[-\frac{9}{2}; -\frac{9}{2}; 1; \left(1 - \frac{r}{R} \right)^2 \right] - 3 \left[\frac{r}{\sigma_{\text{sf}}} \left(2 - \frac{r}{R} \right) \right]^{-4} F \left[-\frac{3}{2}; -\frac{3}{2}; 1; \left(1 - \frac{r}{R} \right)^2 \right] \right] \quad (2)$$

The variables R and r represent, respectively, the effective radius of the cylindrical pore and the distance between the interaction points of the fluid and the wall. The function $F[a; l; x; c]$ denotes the hypergeometric series. The values for the solid parameters used in this work were taken from Ravikovitch et al., $\rho_s = 15.3 \text{ nm}^{-2}$, $\epsilon_s/k_B = 193.1 \text{ K}$ and $\sigma_s = 0.2725 \text{ nm}$.³⁶

The simple surface potential of Tjatjopoulos et al. is considered an appropriate choice to show the suitability of molecular simulations to be used as a tool in process design. The use of this potential for the solid surface avoids additional complexity in the simulated system and saves computational time. Previous works have reported accurate results when using this potential for predicting adsorption isotherms as compared to experimental systems.^{36–41}

The atomistic models employed in the simulations for more realistic materials represent two ordered microporous carbon replicas of siliceous forms of faujasite zeolite (cubic Y-FAU and hexagonal EMT). These atomistic models for ZTC were proposed by Roussel et al.⁴² Simulations of adsorption isotherms for characterizing ZTC using those models materials have been reported previously.^{42,43} The ZTC structures were assumed rigid and the parameters for the carbon atoms in the ZTC were taken to be those customarily used to describe the carbon atoms of graphene sheets, $\epsilon_C = 28.0 \text{ K}$ and $\sigma_C = 0.34 \text{ nm}$.⁴⁴

Simulation Details

The simulation of the adsorption process was done using Grand Canonical Monte Carlo (GCMC) simulations. As this is a standard procedure for molecular simulations of adsorption, the reader is referred to a reference book on the sub-

ject⁴⁵ for details on the simulation procedure, retaining here just the main details concerning the implementation for the particular systems of interest.

The GCMC simulations for the cylindrical pore were done employing: (1) a simulation cell consisting of a cylinder with a diameter ranging from 1.0 to 4.0 nm and a fixed length of 10.0 nm, (2) a cutoff radius of at least 6 times the collision diameter of the fluid molecules (σ_{LJ}),⁴⁶ (3) 1.5×10^5 MC steps for equilibrating the system and 2.0×10^6 MC steps for data collection, (4) an equal a priori probability to displace, insert or remove a molecule in each simulation step and (5) periodic boundary conditions in the z -direction. The parameters ϵ_{ij} and σ_{ij} were calculated from their homonuclear pairs according to the Lorentz Berthelot combining rules.

Experimentally, the pressure of a gas reservoir is imposed on the adsorption system. As the simulations in the confined system are done at fixed chemical potential, comparisons between the results of molecular simulations and experiments require an explicit relationship between the pressure, P , (or the fugacity) of the reservoir and its chemical potential, which can be provided by any accurate equation of state or calculated by simulations of the same force field. In this work, the chemical potential was related to the pressure and the composition in the reservoir by means of the soft-SAFT equation of state, used as an accurate LJ equation of state, fitted to simulation data. For consistency, we fitted the VLE diagrams of each model using the soft-SAFT equation, obtaining slightly different parameters depending on the models; these tuned parameters were used to calculate the chemical potential at different pressures. Although we have used soft-SAFT for this purpose, any other accurate equation of state for these two fluids could be used to relate the pressure to the chemical potential.

The simulation conditions were chosen to mimic the experimental conditions at which this separation takes place. For the thermodynamic conditions, we have used the following values: the compositions for the fluid in the reservoir comprised a serie of values from pure SF₆ to pure N₂, which in terms of SF₆ mole fractions were 0.00, 0.10, 0.25, 0.50, 0.75, 0.90, and 1.00; these values account for the entire composition range. The pressure in the reservoir ranged from 50 to 2000 kPa, we chose this maximum value of pressure, a value below the saturation pressure of pure SF₆, in order to compare the advantages of using adsorption over conventional liquefaction, and as the minimum pressure we used a value close to the atmospheric. Finally, the temperature of the reservoir was fixed at 300 K to simulate adsorption at room temperature.

The simulations of the ZTCs were run at the same thermodynamic conditions than the MCM-41 simulations, except that only two selected representative conditions for the mixture were simulated for the mixture composition: an bulk equimolar mixture of SF₆/N₂, and a mixture with low contents of SF₆ (0.1 mole fraction), as well as both pure fluids. The GCMC simulations were performed on a periodic box containing a unit cell of cubic FAU-ZTC (2.485 nm) and for a hexagonal EMT-ZTC (corresponding to two hexagonal orthorhombic unit cells in x, y directions: $a = 3.4772 \text{ nm}$, $b = 3.0114 \text{ nm}$, and $c = 2.8346 \text{ nm}$). The systems were equilibrated for 1.0×10^6 Monte Carlo steps and 4.0×10^6

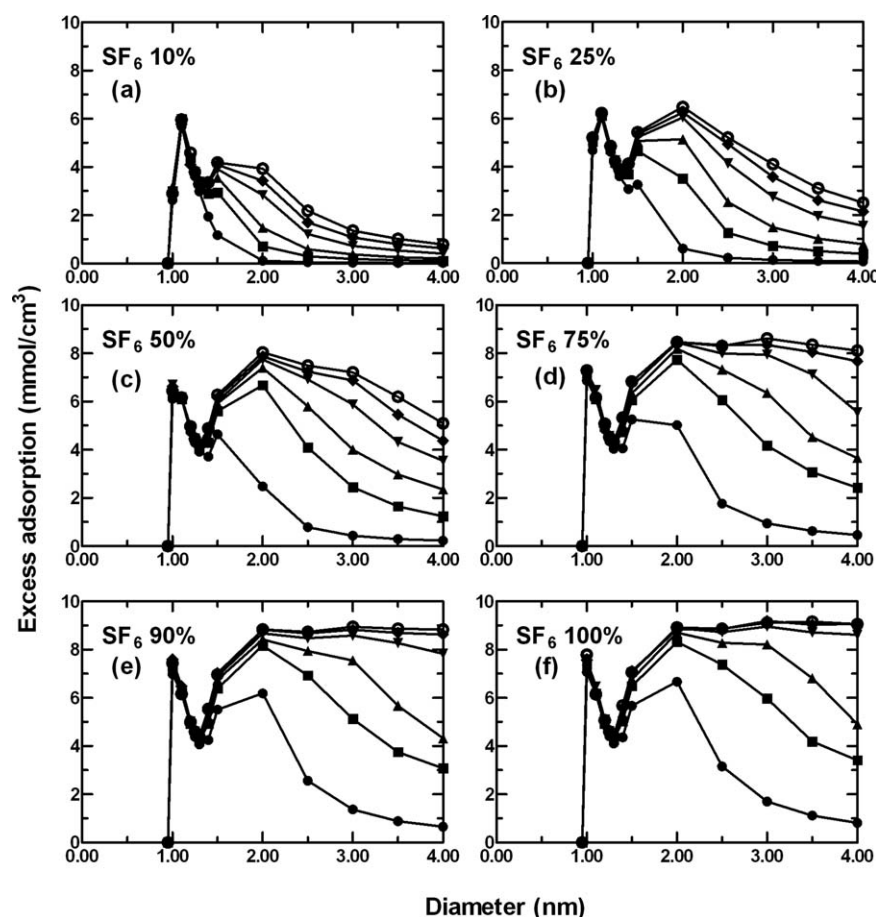


Figure 1. SF₆ excess adsorption isotherms for mixtures of SF₆ and N₂ using a 1-site model. See text for details.

For pressures of 50 kPa (filled circles), 250 kPa (squares), 500 kPa (upward triangles), 1000 kPa (downward triangles), 1500 kPa (rhombs), and 2000 kPa (open circles).

Monte Carlo steps were further performed for averaging purposes. The cut-off radius was taken to be less than half the simulation box length.

Results

We present next the most relevant results divided in three parts: first, the separation of SF₆ from N₂ in MCM-41 considering 1-site models for the fluid and a wide range of pore diameters, pressures, and compositions; second, the separation of the same mixture in the same material at the optimal conditions found in the first case, but considering multisite models for the fluids; and, finally, the separation of the mixture using an atomistic model for the solid.

Separation considering one-site models for the fluids

We present next the adsorption isotherms and the selectivity of MCM-41 for SF₆ and N₂, modeled as a 1-site LJ spheres, using a range of pore diameters from 1.0 nm to 4.0 nm. The results of the GCMC calculations are plotted as excess isotherms (or excess pore density), in order to include only the amount of gas that is adsorbed due to the pore

walls. The excess pore density, ρ_{exc} , is the difference between the absolute density in the pore and the bulk gas density; the absolute density can be defined as the ensemble average of the number of particles per unit of accessible volume.

$$\langle \rho_{\text{exc}} \rangle = \frac{\langle N \rangle}{V} - \rho_{\text{bulk}} \quad (3)$$

The mean number of molecules inside the pore, $\langle N \rangle$, is computed from the GCMC simulations and ρ_{bulk} is the bulk density obtained from the equation of state.

The excess adsorption isotherms for SF₆ at different pore sizes and compositions of the reservoir are shown in Figure 1 (ranging from 1a to 1f, as a function of the mixture composition). The plots show the change in the adsorption behavior going from a diluted gas mixture, 0.1 mole fraction of SF₆ in Figure 1a, to pure SF₆, in Figure 1f.

Two important characteristics of the adsorption behavior can be extracted from the SF₆ adsorption isotherms. First, there is an inflection point at a pore diameter of 2.0 nm: the effect of the composition on the adsorption of SF₆ behaves differently above and below this size. For pore diameters

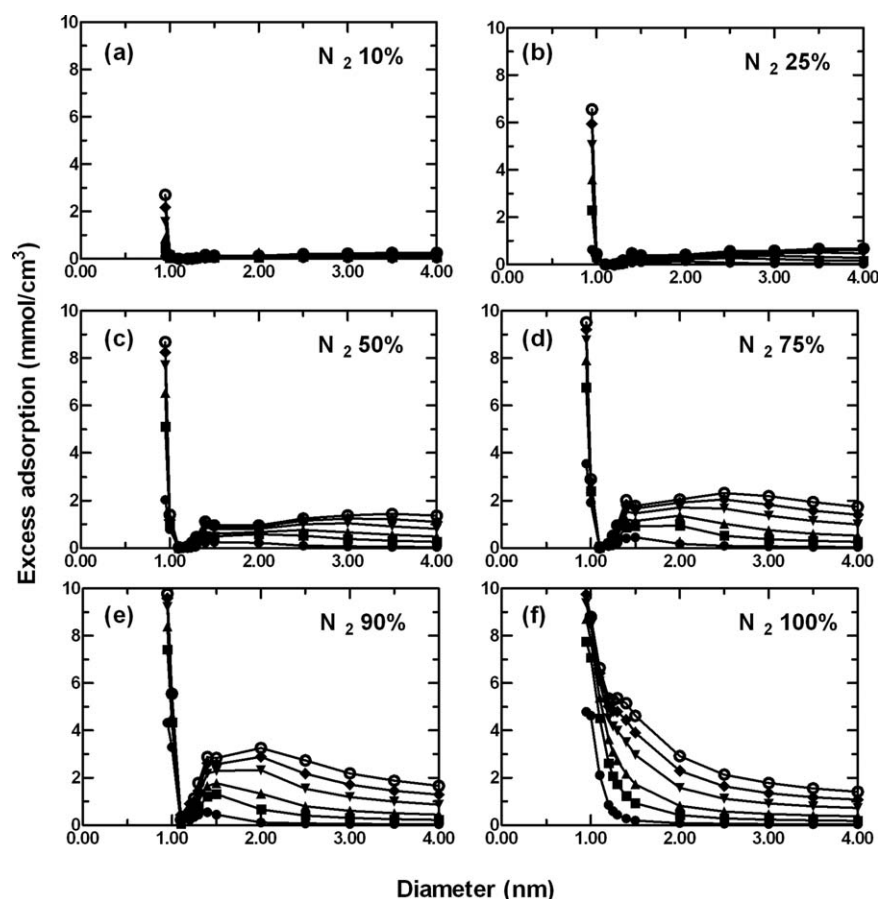


Figure 2. N_2 excess adsorption isotherms for mixtures of SF_6 and N_2 using a 1-site model.

Symbols as in Figure 1.

smaller than 2.0 nm the amount of SF_6 adsorbed is a weak function of the composition. Even at low molar fractions of SF_6 , its behavior is similar to pure SF_6 . Moreover, for larger pore sizes, it diminishes when the concentration of N_2 in the bulk increases. This indicates that SF_6 is strongly attracted towards the wall. The fluid–solid interactions weaken when the loading increases, as more molecules are forced to remain in the center of the pore, where the attraction due to the walls is smaller.⁴⁷ The second characteristic is, that for all the diameters studied, a pressure of 2000 kPa saturates the pore with pure SF_6 , see Figure 1f. Hence, the point of maximum adsorption, which is an indication of the capacity of the solid material, is reached at low pressures. The 1-site model for SF_6 predicts that the fluid-wall interactions are very strong and the pores are filled up at low pressures. This is also seen in the excess isotherm plots at SF_6 mole fractions above 0.75, Figures 1d–f, which are almost equal; at high contents of SF_6 the isotherms behave almost as if it was pure SF_6 . This is a typical behavior for the larger molecule in the adsorption of binary mixtures: at the lowest relative pressures, the larger molecule is strongly attracted to the wall and it saturates the pore faster than the smaller molecule.^{48,49}

The excess adsorption isotherms for N_2 at different pore sizes and initial bulk compositions are depicted in Figure 2. The adsorption isotherms of N_2 show a strong influence of

the composition on the adsorbed amount, this might be due to the SF_6 molecules being more attracted towards the wall and blocking the space for N_2 adsorption. For pore diameters larger than 2.0 nm the adsorption of N_2 is very low for the pressure range analyzed. For a pore size of 1.0 nm, N_2 is strongly adsorbed, due to the confinement, when the mole fraction of SF_6 is small; once SF_6 concentration starts to increase, the adsorbed amount of N_2 diminishes abruptly. This sudden decline of N_2 adsorption is due to the larger SF_6 molecule entering the small pore occupying almost all the free space, making it harder for the N_2 molecules to adsorb. The lessening of N_2 adsorption with increasing content of SF_6 weakens at larger pore diameters. This might be due to the fact that the adsorbed SF_6 molecules near the solid wall create an attractive energy that facilitates adsorption of N_2 , e.g., for a diameter of 4.0 nm the adsorbed amount of N_2 with 0.25 mole fraction of SF_6 is higher than it is for pure N_2 .

An advantage of using molecular simulations is the additional microscopic information provided by them, as one is able to locate the molecules in their equilibrium configurations, as shown in Figure 3 for different pore diameters. The adsorption isotherms illustrate that at 1.1 nm the amount of adsorbed N_2 is negligible. As observed in Figure 3b, the exclusion of N_2 in the pore of 1.1 nm is due to the SF_6

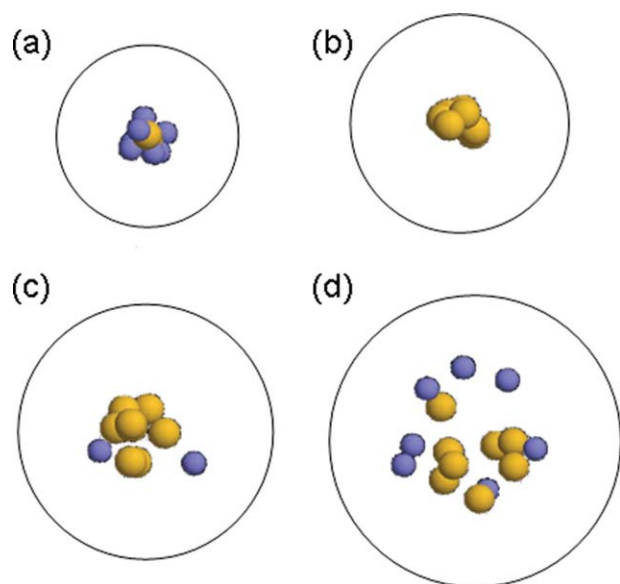


Figure 3. Snapshots of adsorbed SF₆ and N₂ at different pore sizes for mixtures with a molar fraction of SF₆ of 0.10.

Pore diameters (a) 1.0 nm, (b) 1.1 nm, (c) 1.2 nm, and (d) 1.3 nm. SF₆ is represented in yellow and N₂ is represented in blue. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://www.interscience.wiley.com).]

molecules, more strongly attracted toward the solid, accommodated in an alternating fashion. At smaller pore diameters (see Figure 3a) SF₆ accommodates in a straight line because of the strong effect of the pore walls, and N₂ molecules can distribute around the SF₆ molecules. Although for pore diameters larger than 1.1 nm (see Figures 3c, d) the SF₆ is distributed in a similar way but these larger pore sizes allow enough free space for N₂ to adsorb. Hence, for the 1.1-nm pore the SF₆ molecules distribute in such a way that the free space among SF₆ molecules and the solid walls is not large enough for N₂ molecules to fit, thus SF₆ selectively adsorbs, excluding almost completely, the N₂ molecules. This exclusion of the smaller molecule was first predicted by Sommers et al.,⁵⁰ for two spherical particles of different sizes in slit pores. This effect is more pronounced due to the simple geometry of the force fields, modeling the molecules as spheres, thus they are not allowed to rotate and find free space within the pore to be adsorbed.

Regarding the separation of the mixture as a function of composition, Figure 2 shows that for SF₆ mole fractions above 50% the amount of N₂ adsorbed is very small, thus it is a simple task to separate an enriched mixture of SF₆ with N₂, as pointed out by Inami et al.⁸ They claimed that this enriched mixture could be separated by compressing and cooling the gas. The advantage of using adsorption, as done

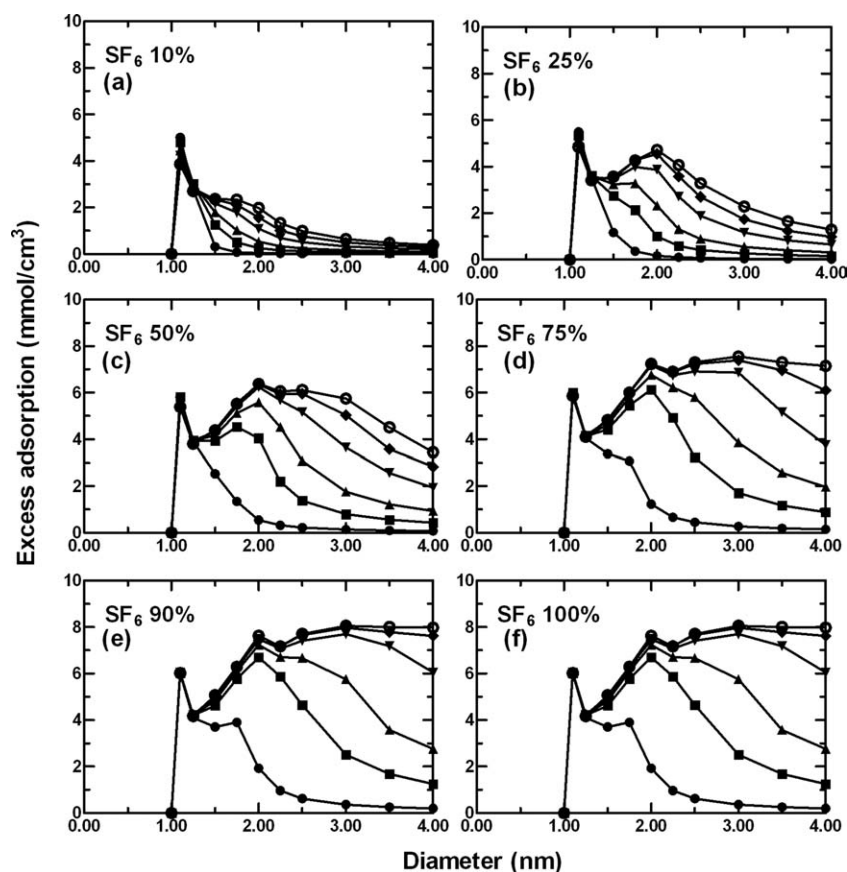


Figure 4. SF₆ excess adsorption isotherms for mixtures of SF₆ and N₂ using multisite models for the fluids. See text for details.

Symbols as in Figure 1.

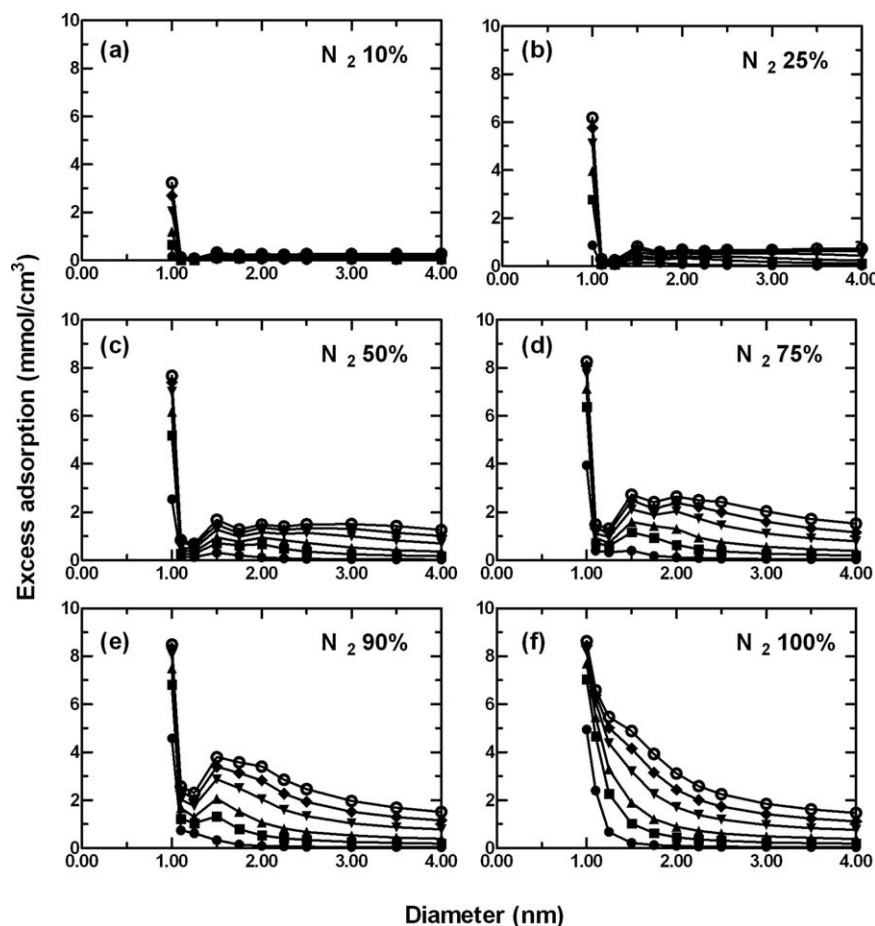


Figure 5. N₂ excess adsorption isotherms for mixtures of SF₆ and N₂ using multisite models for the fluids.

Symbols as in Figure 1.

in this work, is that using an adsorbent, as shown here, overcomes the difficulty of recovering SF₆ from the gas mixture lies in the separation of SF₆ from diluted mixtures, once the proper diameter for effective separation is found.

At higher pressures, N₂ starts to adsorb in the pore and begins to displace SF₆, compared to the adsorption of pure SF₆. This competitive adsorption effect has been observed in other binary mixtures, such as the mixture of CO₂ and N₂ in metal-organic frameworks, where CO₂ is preferentially adsorbed at low pressures but it is displaced by N₂ at higher pressures.⁵¹ For instance, for a SF₆ molar fraction of 0.1, the amount of SF₆ adsorbed at 1.5 nm reaches a plateau before 1000 kPa, further increasing the pressure only increases the adsorbed amount of N₂. This competitive behavior is due to the nonideal behavior of SF₆ at higher pressures, as at these conditions the fugacity of SF₆ starts to deviate from the ideal behavior, while N₂ acts almost as an ideal gas. Thus, the fugacity of SF₆ does not increase as steeply with pressure as it does for N₂; therefore it becomes increasingly easier to adsorb N₂ molecules as the acceptance rule for the creation of new molecules directly depends on the fugacity.⁵²

The selectivity is the preference of one substance over the other (or others) in the mixture to stay in a given phase; for adsorption processes, it is desirable to have a high selectivity

of the substance to be separated. For SF₆ and N₂ in any adsorbent the selectivity is defined as:

$$S_{\text{SF}_6-\text{N}_2} = \frac{x_{\text{SF}_6}/x_{\text{N}_2}}{y_{\text{SF}_6}/y_{\text{N}_2}} \quad (4)$$

The selectivity of SF₆ over N₂ is $S_{\text{SF}_6-\text{N}_2}$, where x_{SF_6} and x_{N_2} are the mole fractions of the two components on the adsorbent surface; y_{SF_6} and y_{N_2} are the corresponding mole fractions in the bulk. Values of selectivity larger than one mean that SF₆ is preferentially adsorbed over N₂.

According to Babarao et al. simulations are useful for estimating the general trend of the selectivity, but its value cannot be accurately assessed solely from molecular simulations, as small deviations in the number of molecules might result in a large change in the selectivity.⁵³ The results of the selectivity using the 1-site model do not present meaningful information in this case, as the complete exclusion of the N₂ molecules for a pore diameter of 1.1 nm makes the selectivity for that pore diameter to tend to infinity. However, for an adsorbent it is important to have both high adsorption capacity and selectivity. The adsorption capacity for a pore diameter of 1.1 nm is among the highest for the pressure range analyzed, and due to the exclusion of N₂ at

this pore size the MCM-41 adsorbent is highly selective toward the adsorption of SF₆.

To assess the reliability of these results from molecular simulations we have further investigated this case (pore diameter of 1.1 nm), using a more refined force field for the fluid, which takes into account details of the molecular structure of the molecules, expecting that this should have an effect on the adsorption. Results are presented in the next subsection.

Separation considering multisite models for the fluids

Once a throughout study with the optimal conditions for separation was performed with simple models, we have carried out additional simulations using multisite models to confirm the results and test the reliability of the 1-site model for optimizing process equipment for these mixtures and material. Of special interest to the present study is the pore diameter close to 1.1 nm, given the results obtained for the 1-site model.

As aforementioned in the model section, multisite models have additional degrees of freedom with respect to the 1-site model: multisite molecules can change their orientation and, in the case of flexible models, the bonds and angles can vibrate. SF₆ is a highly symmetric molecule that can be represented by a spherical model, with either 1-site or multisite. Whereas N₂ is a linear molecule; it has been discussed the problems in interpretation and predictions resulting of using a 1-site model for a linear molecule.^{54,55} The introduction of these changes in the molecular models has a significant effect on the adsorption behavior of pure components, especially at diameters where the adsorption begins its transition from monolayer to multilayer.⁵⁴ As the simulations for the 1-site models gave an optimal adsorption diameter of 1.1 nm, this diameter lies within this transition range⁵⁶ and it is worthy further investigating it with the more refined fluid models. It is expected that the results differ from those obtained with the 1-site spherical LJ models mainly because of the nature of N₂, but also because of the additional details introduced for the SF₆ molecule.

The adsorbed amount of SF₆ predicted by the multisite models is depicted in Figure 4. The most noticeable characteristic of these plots, compared to Figure 1, is the lack of adsorption of SF₆ at 1.0 nm; SF₆ molecules of the multisite model cannot fit in the 1.0 nm pores. This behavior is also seen in the 1-site models for a pore diameter of 0.95 nm.

The maximum capacity, for the pressure range studied, is reached for a pore diameter of 2.0 nm, as observed for the 1-site model. The main difference between Figures 1 and 4 is the total amount of SF₆ adsorbed in the material; it is smaller for the multisite model than for the 1-site one, especially at low SF₆ molar fractions. Another important difference between the two sets of results is the slope of the isotherms. The 1-site model has a steeper slope than the multisite one, due to the differences in the geometry of the molecules.

The adsorbed amount of N₂ predicted with the multisite models is depicted in Figure 5. The adsorption of N₂ molecules obtained when using the multisite model is not as affected by the presence of SF₆ molecules as it was for the 1-site model, hence, the decrease in the adsorption of N₂

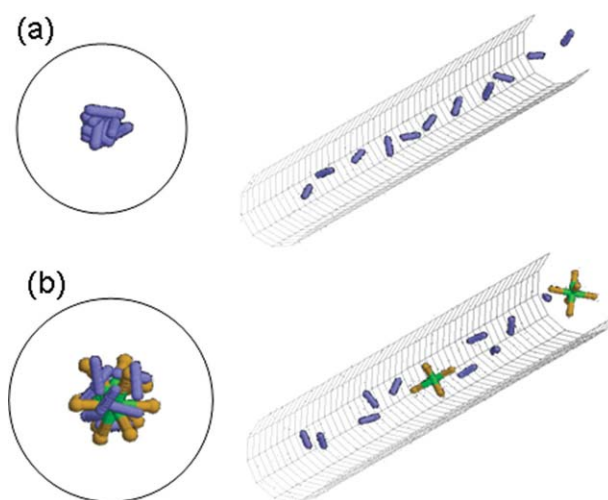


Figure 6. Snapshots of adsorbed SF₆ and N₂ at different pore sizes with a molar fraction of SF₆ of 0.10.

Pore diameters (a) 1.0 nm and (b) 1.1 nm. N₂ is represented in blue while SF₆ is represented in yellow (the F atoms) and green (the bonds between atoms). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

with the presence of SF₆ molecules is less marked. Additional insights into this effect can be inferred by looking at the equilibrated configurations, shown on Figure 6. In the 1.0-nm pore, only N₂ molecules can get inside the pore and SF₆ molecules are excluded, as seen in Figure 6a. Figure 6b shows the local minimum for the adsorption of N₂ observed at 1.1 nm. SF₆ molecules block a large portion of the free volume for the adsorption of N₂, although in this case, because of the linear geometry 2-site model, N₂ molecules can rotate and accommodate to find free space in the narrow pore.

The competitive adsorption of N₂ at higher pressures is seen better for the multisite models than for the LJ model, partially due to the fact that the amount of adsorbed SF₆ is lower in this case, and also because the linear N₂ molecules pack more easily near the pore wall, being able to adsorb more than the spherical ones at lower pressures.

The local minimum observed in the N₂ adsorption for a pore diameter of 1.1 nm (for molar fractions of N₂ below 0.75) is also reflected in the selectivity plots shown in Figure 7; the maximum selectivity is reached at this point of minimum N₂ adsorption. This optimum selectivity occurs at a pore size where SF₆ blocks the free space for the adsorption of N₂, enhancing the separation of their molecules. This effect diminishes with pressure, because the higher pressures favors the competition between SF₆ and N₂ and also the packing of the molecules increases, creating more small accessible free spaces.⁵⁷ Furthermore, the minimum adsorption (a local minimum) for SF₆ is found at 1.5 nm, which is reflected in the selectivity plot as the minimum in selectivity. This selectivity minimum is the point where the transition from a single to multiple layers of SF₆ is achieved.

The selectivity follows the trend predicted by the theoretical analysis in a one-dimensional system performed by Talbot.⁴⁸ The larger molecule is attracted in a stronger manner

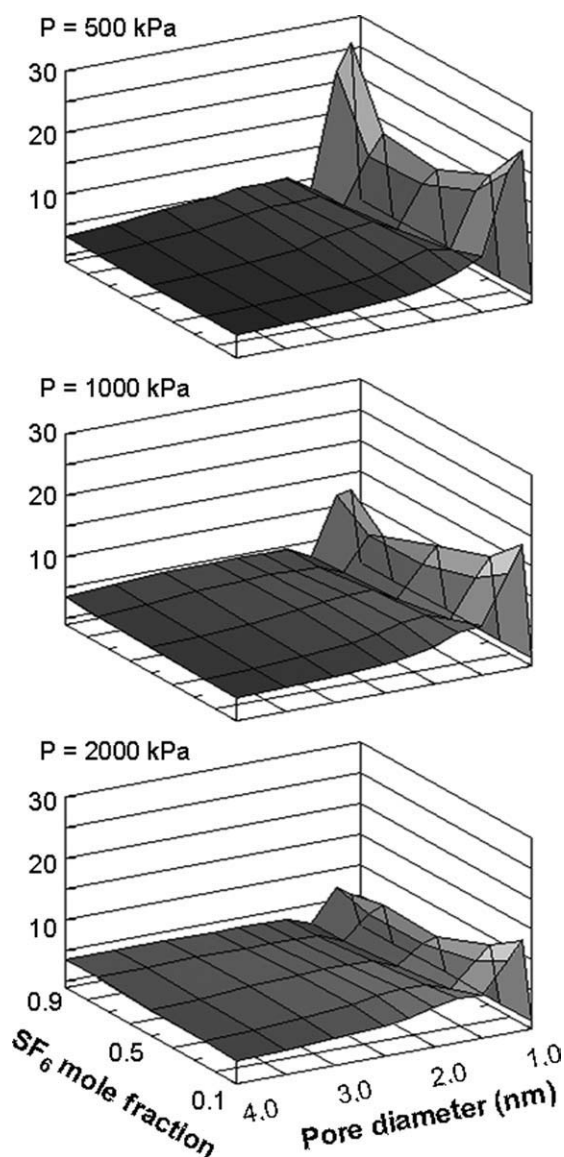


Figure 7. Selectivity of SF_6 over N_2 using multisite models.

to the solid material. For pressures below the iso-selective point the composition has a strong influence on the selectivity, while when approaching the isoselective point, increasing the pressure reduces the differences among the different compositions. It is also worth noting that a decrease of the selectivity with pressure for all compositions is achieved due to the competitive adsorption already discussed. At low pressures (see Figure 7a), the material is more selective towards SF_6 than at higher pressures, because a competitive adsorption with N_2 that takes place at higher pressures.

Finally, in a similar fashion to the 1-site model, the selectivity is independent of pore size and composition for pores wider than 2.0 nm, due to the free volume available for both molecules to adsorb, whereas the selectivity decreases with pressure, because of the competitive adsorption and the packing effect of N_2 . This independency of selectivity with pressure has been observed for other solid adsorbents with large pore sizes and high volumetric capacity, such as a mixture of CH_4/H_2 in non-interpenetrated MOFs.^{47,58}

Separation using an atomistic model for the solid

As a final step in this study, once the optimal conditions for separation were found with the simple models, and these conditions corroborated with the refined force fields for the fluid, we have checked the performance of a realistic material with a pore diameter similar to the one found for optimal separation, to check its performance for separating this mixture. For this purpose, we have used two different solid materials with different shapes and similar pore sizes: (1) FAU-ZTC, which has a sharp pore size distribution located around 1.1–1.2 nm, and (2) EMT-ZTC, which has a bimodal and wider pore size distribution around 0.8–1.1 nm.^{27,42} Snapshots of both structures are presented in Figure 8 while details on the materials can be found in the original references.^{27,42}

Although the values for the adsorption isotherms should be different from those of the silica cylindrical model, ordered materials with almost cylindrical structures, such as zeolites or zeolite carbon replicas, should follow the general trend observed with the ideal cylindrical pore.

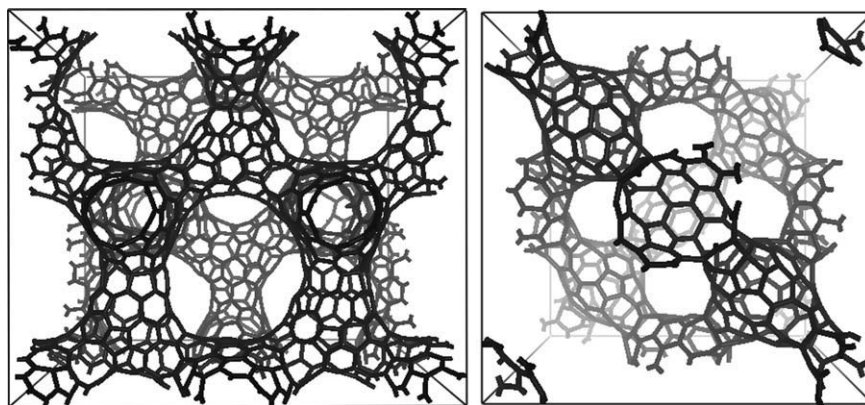


Figure 8. Models of the atomistic structures: EMT-ZTC (left) and FAU-ZTC (right).

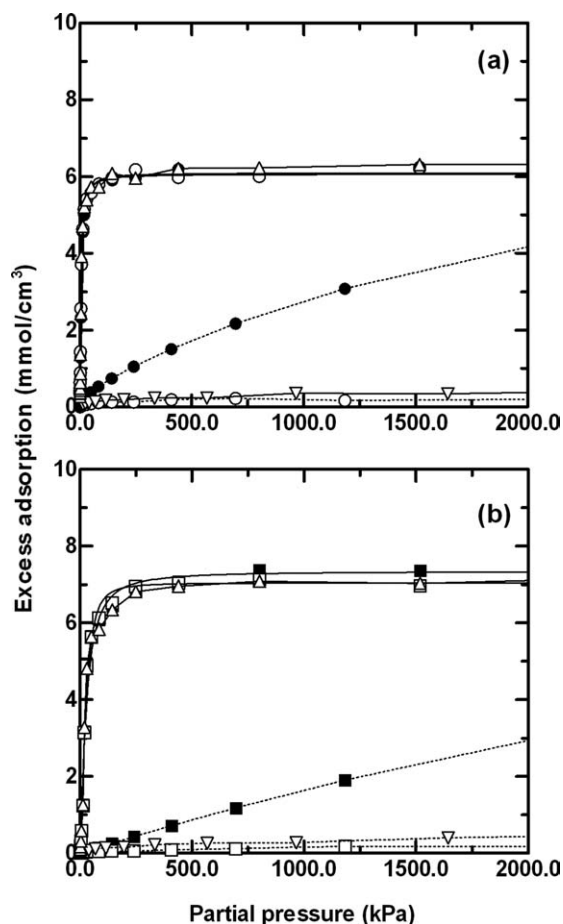


Figure 9. Adsorption isotherms of pure SF₆, pure N₂ (closed symbols, full, and dashed line respectively), SF₆, and N₂ in an equimolar mixture in the bulk (open symbols, full and dashed line respectively), and SF₆ and N₂ in a mixture with 0.1 molar fraction of SF₆ (upward and downward triangles, respectively) on EMT-ZTC (a) and FAU-ZTC (b) as function of the partial pressure of each fluid.

The adsorption isotherms of SF₆ and N₂ on ZTC materials, as a function of the partial pressure of each substance, are depicted in Figure 9. It can be observed in the figure how N₂ is displaced by SF₆ during the adsorption on both EMT-ZTC (Figure 9a) and FAU-ZTC (Figure 9b). The adsorption isotherms for pure SF₆ are almost identical to the isotherms of SF₆ in the mixture, whereas for N₂ the adsorption isotherms of the pure fluid are far higher than when SF₆ is present. The amount of SF₆ adsorbed on FAU-ZTC (the material with a sharp pore size distribution at the desired pore size) is higher than for EMT-ZTC, and the opposite behavior is observed for N₂. This behavior means excellent efficiency for the separation on FAU-ZTC, as confirmed by the selectivity plots depicted in Figure 10. For pressures between 100 and 1000 kPa on FAU-ZTC an optimal separation efficiency is achieved, with selectivity values around

130, much higher than any other previously reported material for this mixture separation.

The slope of the adsorption isotherms is steeper for EMT-ZTC; this means that the solid–fluid interactions are stronger in this material. This is reflected in the selectivity, which decreases with increasing pressure for EMT-ZTC, while for FAU-ZTC the selectivity first increases until a certain pressure, and then it begins to decrease with pressure; at this point, the total capacity for SF₆ adsorption has been reached and the competitive adsorption of N₂ begins to displace some SF₆.

The predictions of the optimal diameter show that FAU-ZTC is an excellent technical option for separating SF₆/N₂ mixtures. This can be seen by comparing the values of the selectivity for FAU-ZTC (and even EMT-ZTC) to the ones reported in the literature. Experimentally, for inlet compositions of 0.10 mole fraction of SF₆ on a Ca-A zeolite a selectivity of 28.5 was obtained,¹⁰ likewise a selectivity of 44.3 on a Na-X type zeolite¹¹ and a selectivity of 12.8 was obtained on Vycor glass.¹² In addition, the best adsorbent material in terms of selectivity, found in the literature (Na-X zeolite) has an average pore size of 1.0 nm. This confirms the results of our simulations, with the cylindrical model, for the optimal pore diameter. It is important to note that the values reported in the literature are equivalent to a dynamical separation process, whereas the values reported here are equivalent to a fixed value at a certain composition. We report the values of our simulations for a molar fraction of SF₆ of 0.5 to take into account this difference. At low SF₆ concentration in the bulk, the selectivity is even greater.

Given the comparison with the other materials for SF₆/N₂ separations, the carbon replicas used here show a very promising capability for separating SF₆/N₂ mixtures from a practical point of view, especially FAU-ZTC. The mechanical properties of ZTC would allow the separation using a device as the one portrayed by Murase et al.¹¹ as a way feasible to separate and store SF₆ for its recovery and reutilization.

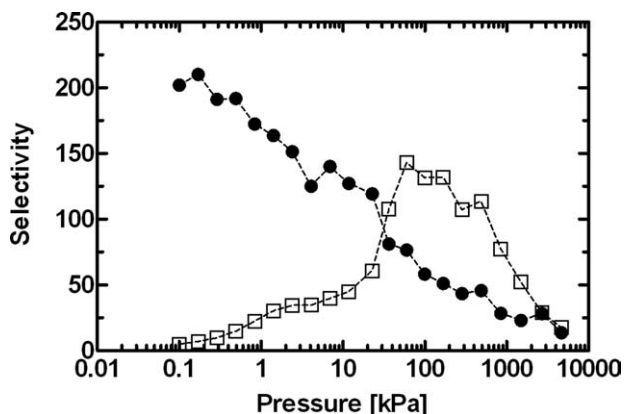


Figure 10. Selectivity of SF₆ over N₂ on EMT-ZTC (circles) and FAU-ZTC (squares) for a bulk equimolar mixture.

Conclusions

This study illustrates how molecular simulations can be used to guide the selection for the optimal conditions for separations of mixtures by adsorption, and how an optimal material can be found following this procedure. The methodology has been applied to separate, by adsorption, sulfur hexafluoride (SF₆) from nitrogen (N₂), a mixture of key interest for electrical applications, and a separation needed to avoid the emission of SF₆ into the atmosphere.

We have first studied the influence of composition, pressure and pore diameter on the adsorption and separation of SF₆ and N₂ mixtures in MCM-41 by using GCMC molecular simulation as a way to optimize the separation process. Results show that the maximum selectivity by adsorption is obtained for a cylindrical pore diameter of 1.1 nm; where sulfur hexafluoride molecules block the empty volume of the pore and prevent nitrogen from being adsorbed. The importance of using molecular simulation to find the optimum value is clearly shown by the narrow range of pore diameters with high selectivities; in addition, simulations help to visualize the distribution and orientation of the molecules at the molecular level. It has been obtained that the selectivity is almost independent of the pore diameter and the mixture composition for pore diameters larger than 2.0 nm, due to the free available volume for the two components. Further simulations with more refined force fields for the fluids, including geometrical information and flexibility of the molecules, mainly corroborate the optimal conditions for separation obtained with the simple models.

Once the optimal pore diameter for separation in the simple MCM-41 model material was found, additional simulations were performed in ordered materials with almost cylindrical structures, such as zeolite carbon replicas (Zeolite Templated Carbons, ZTC). GCMC simulation results show very high selectivities for FAU-ZTC and EMT, being the selectivity higher for FAU-ZTC, a material with a narrow pore size distribution located around 1.1 nm. Selectivities found for this material are approximately four times higher than the best material for separation published in the open literature. Given the mechanical properties of these carbon replicas, these materials show a great potential for applications in recovering SF₆ from SF₆/N₂ mixtures present in gas-insulated equipment.

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